

$$\lim_{x \rightarrow 0} \sin x \cdot (\ln x)^2 = \lim_{x \rightarrow 0} \frac{\frac{1}{\sin x} \cdot \sin x \cdot (\ln x)^2}{\frac{1}{\sin x}} = \lim_{x \rightarrow 0} \frac{(\ln x)^2}{\left(\frac{1}{\sin x}\right)} \rightarrow \left\{ \frac{\infty}{\infty} \right\} =$$

$$= \lim_{x \rightarrow 0} \frac{\frac{2 \ln x}{x}}{\frac{-\cos x}{\sin^2 x}} = \lim_{x \rightarrow 0} \frac{\frac{2 \ln x}{x}}{\frac{-\cot x}{\sin x}} = \lim_{x \rightarrow 0} \frac{2 \ln x \cdot (\sin x)}{\cot x \cdot x} \rightarrow 1 =$$

$$= \lim_{x \rightarrow 0} \frac{2 \ln x}{\cot x} \rightarrow \left\{ \frac{\infty}{\infty} \right\} = \left(\frac{\frac{2}{x}}{-\frac{1}{\sin^2 x}} \right) = - \lim_{x \rightarrow 0} \frac{2 \sin^2 x}{x} =$$

$$\lim_{x \rightarrow 0} \frac{2 \sin x \cdot \sin x}{x} = \lim_{x \rightarrow 0} 2 \sin x = 0$$